

# Double Feature:

**Secure Two-Party Threshold ECDSA  
from ECDSA Assumptions**

**Threshold ECDSA from ECDSA  
Assumptions: the Multiparty Case**

**Jack Doerner** • Yashvanth Kondi • Eysa Lee • abhi shelat

2016

2020

[DKLs18]

[DKLs19]



[GGN16]

[Lin17]

[BGG17]

[DKLs18]

[DKLs19]

2016

2020



[GGN16]

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[GGN16]

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[GG18]

[DKLs19]

[CCLST19]

[DOKSS19]

[CCLST20]

[CMP20]

[GKSS20]

[DJNPØ20]

[GG20]

2016

2020

# 14 Papers!

[GGN16]

[Lin17]

[BGG17]

[DKLs18]

[LNR18]

[GG18]

[DKLs19]

[CCLST19]

[DOKSS19]

[CCLST20]

[CMP20]

[GKSS20]

[DJNPØ20]

[GG20]

2016

2020

# *14 Papers!*

*After 7 followups, we still stand out*

[GGN16] [Lin17] [BGG17] [DKLs18] [LNR18] [GG18] [DKLs19] [CCLST19] [DOKSS19] [CCLST20] [CMP20] [GKSS20] [DJNPØ20] [GG20]

2016

2020

**Threshold ECDSA  
From ECDSA Assumptions**

**[DKLs18] [DKLs19]**

**OT-Based**

**Preproc All But Last Msg**

**Securing DNSSEC Keys  
via Threshold ECDSA  
From Generic MPC**

**[DOKSS19]**

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**No EC Abstraction**

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**2 Msgs for 2 Parties**

**Many Optimizations**

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**2 Msgs for 2 Parties**

**Many Optimizations**

**Better 2P Perf**

**More Complex Proof**

**Securing DNSSEC Keys  
via Threshold ECDSA  
From Generic MPC**

[DOKSS19]

**OT-Based**

**Preproc All But Last Msg**

**Nice EC Abstraction**

**Good 2P Perf**

**Simpler Proof**

# OT vs HE

[GGN16]  
[Lin17]  
[BGG17]  
[DKLs18]  
[LNR18]  
[GG18]  
[DKLs19]  
[CCLST19]  
[DOKSS19]  
[CCLST20]  
[CMP20]  
[GKSS20]  
[DJNPØ20]  
[GG20]

# OT vs HE

Paillier + ZK:

[DKLs18]

[GGN16]

[Lin17]

[BGG17]

[LNR18]

[GG18]

[CMP20]

[GKSS20]

[GG20]

[DKLs19]

[CCLST19]

[DOKSS19]

[CCLST20]

[DJNPØ20]

# OT vs HE

CG + HPS:

[CCLST19]  
[CCLST20]

Paillier + ZK:

[GGN16] [Lin17] [BGG17] [LNR18] [GG18] [CMP20] [GKSS20] [GG20]  
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# OT vs HE

CG + HPS:

[CCLST19]  
[CCLST20]

Paillier + ZK:

[GGN16] [Lin17] [BGG17] [LNR18] [GG18] [CMP20] [GKSS20] [GG20]

OT:

[DKLS18] [DKLS19] [DOKSS19]

Paillier + ZK

OT

# Paillier + ZK

Low Communication

# OT

# Paillier + ZK

Low Communication

Extra Assumptions

# OT

# Paillier + ZK

Low Communication

Extra Assumptions

Very High Computation

# OT

# Paillier + ZK

# OT

**Low Communication**

**Extra Assumptions**

**Very High Computation**

**NIZK over Crypto**

# Paillier + ZK

Low Communication

Extra Assumptions

Very High Computation

NIZK over Crypto

# OT

High Communication

Native Assumptions

Low Computation

No ZK

# OT

**High Communication**

**Native Assumptions**

**Low Computation**

**No ZK**

Not so bad, actually



# Example 1: Mobile Wallet

Multiplier: OT-based

Parties: 4

Curve: 256-bit

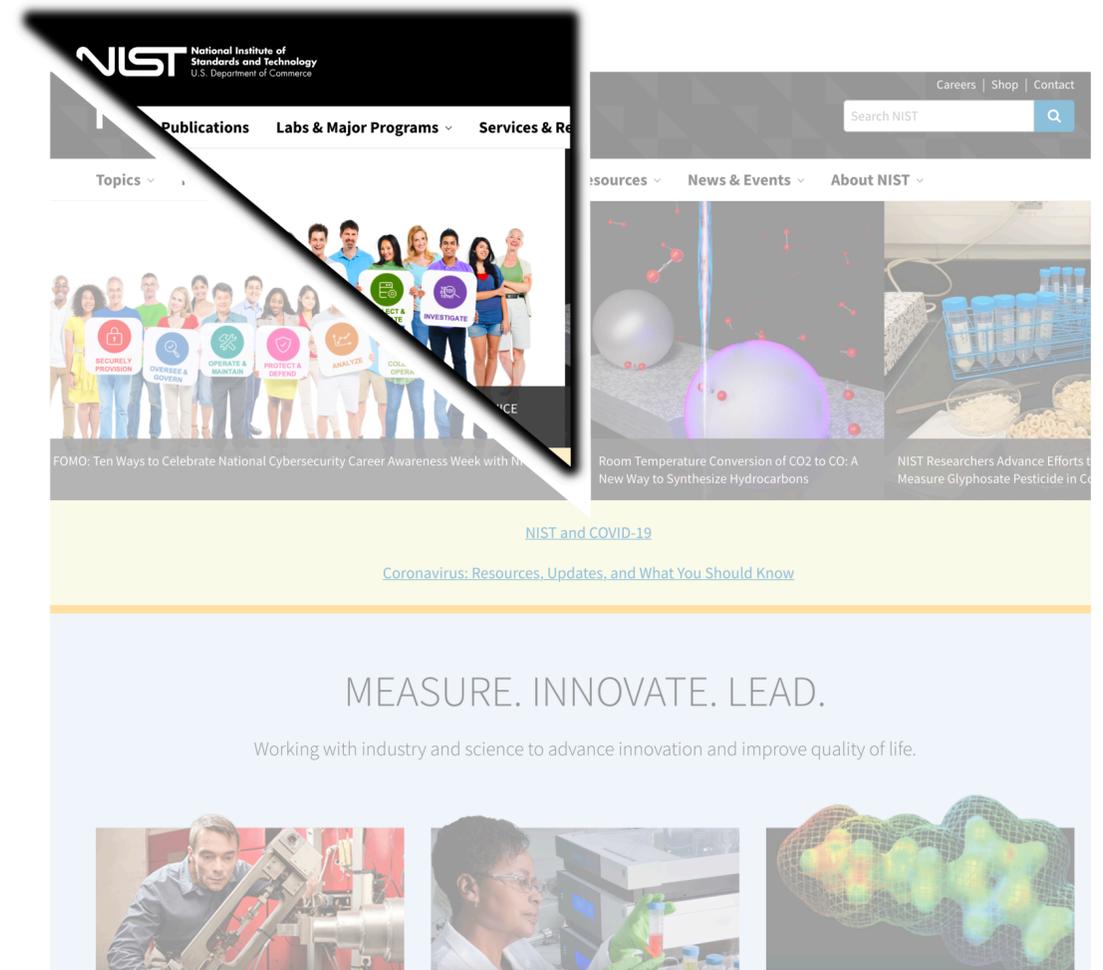
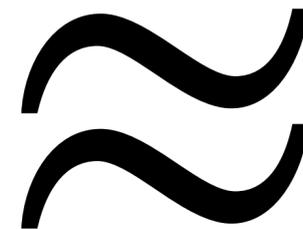
2 Mbits

sent per party

# Example 1: Mobile Wallet

Multiplier: OT-based  
Parties: 4  
Curve: 256-bit

2 Mbits  
sent per party



# Example 1: Mobile Wallet

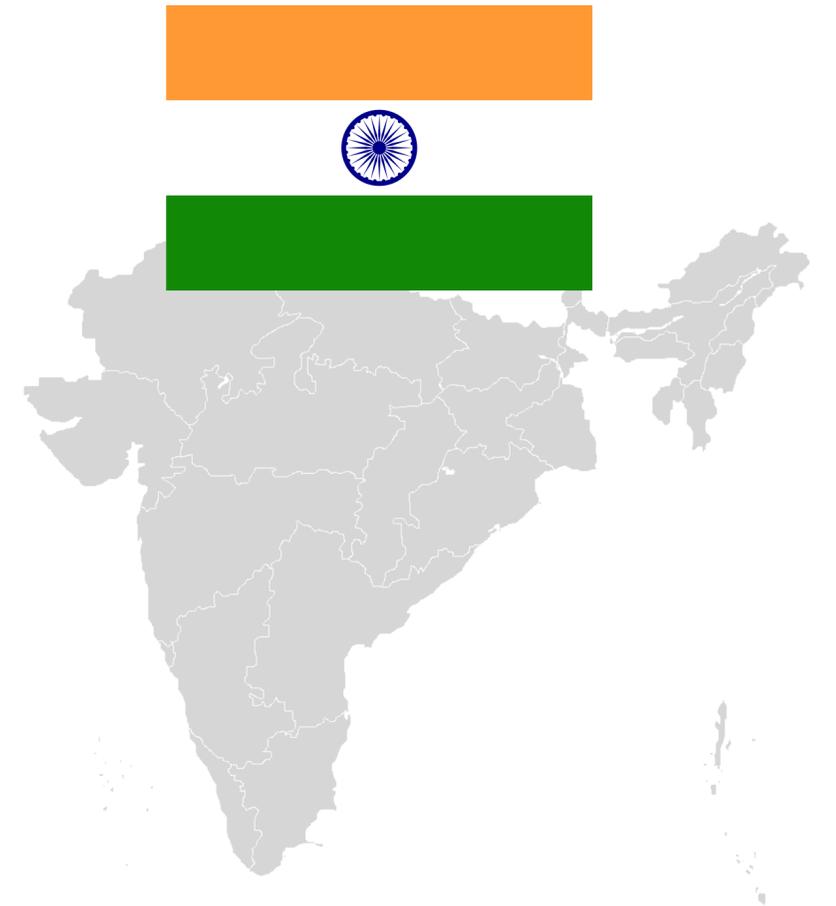
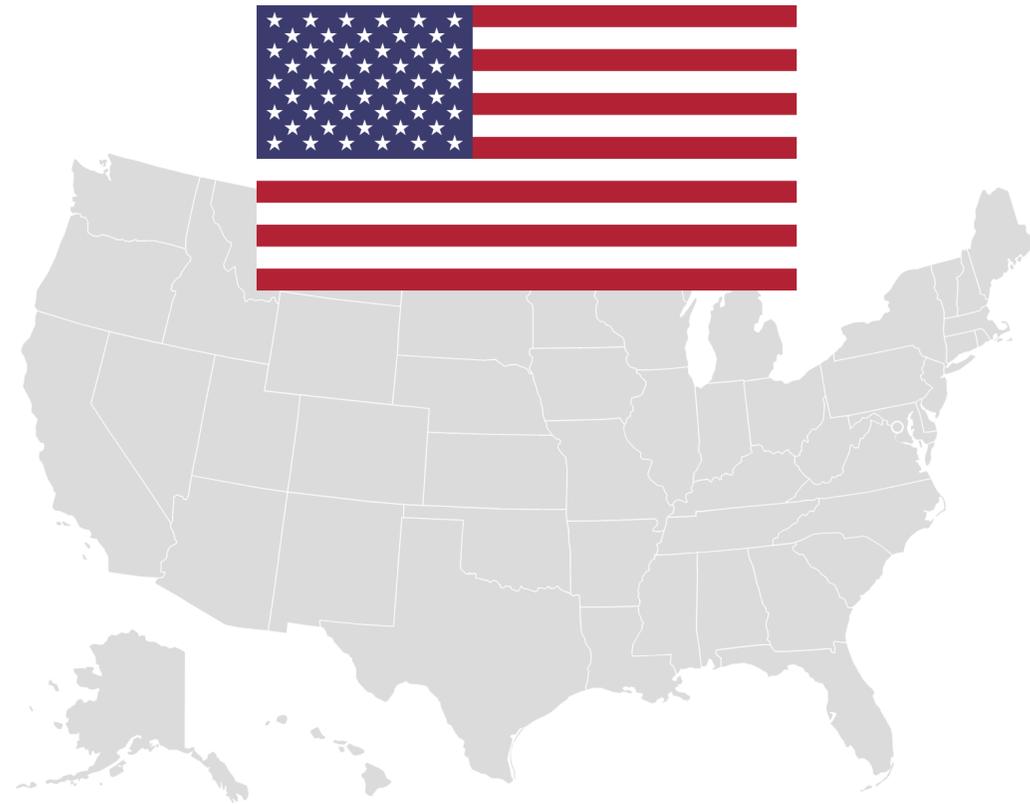
**Multiplier: OT-based**

**Parties: 4**

**Curve: 256-bit**

**2 Mbits**

**sent per party**



# Example 1: Mobile Wallet

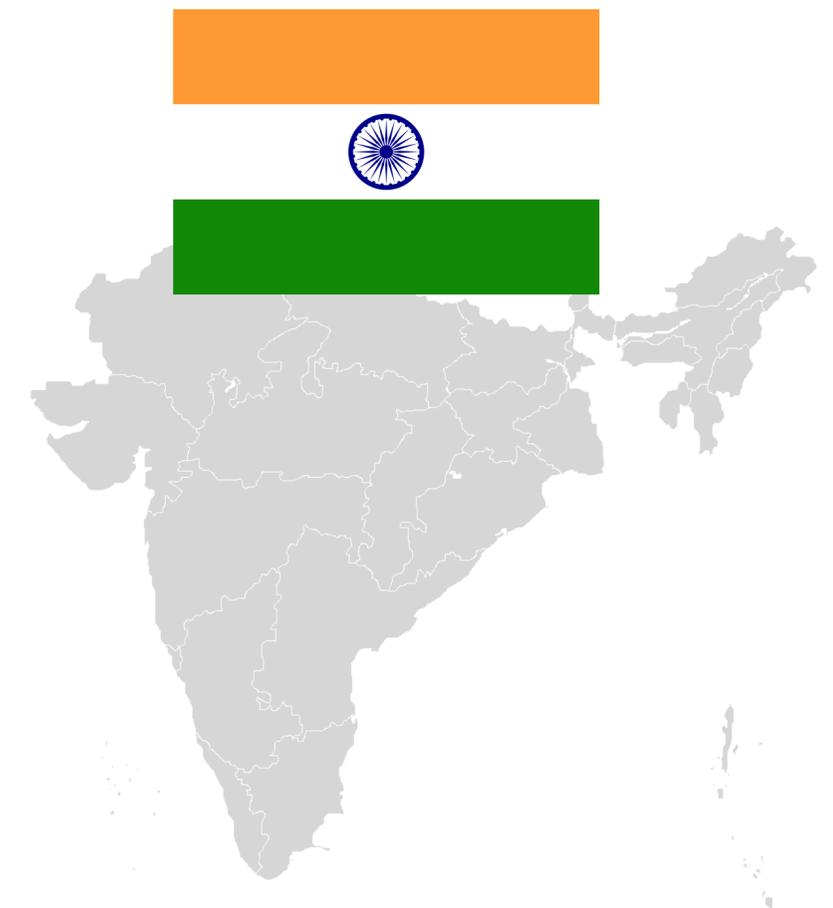
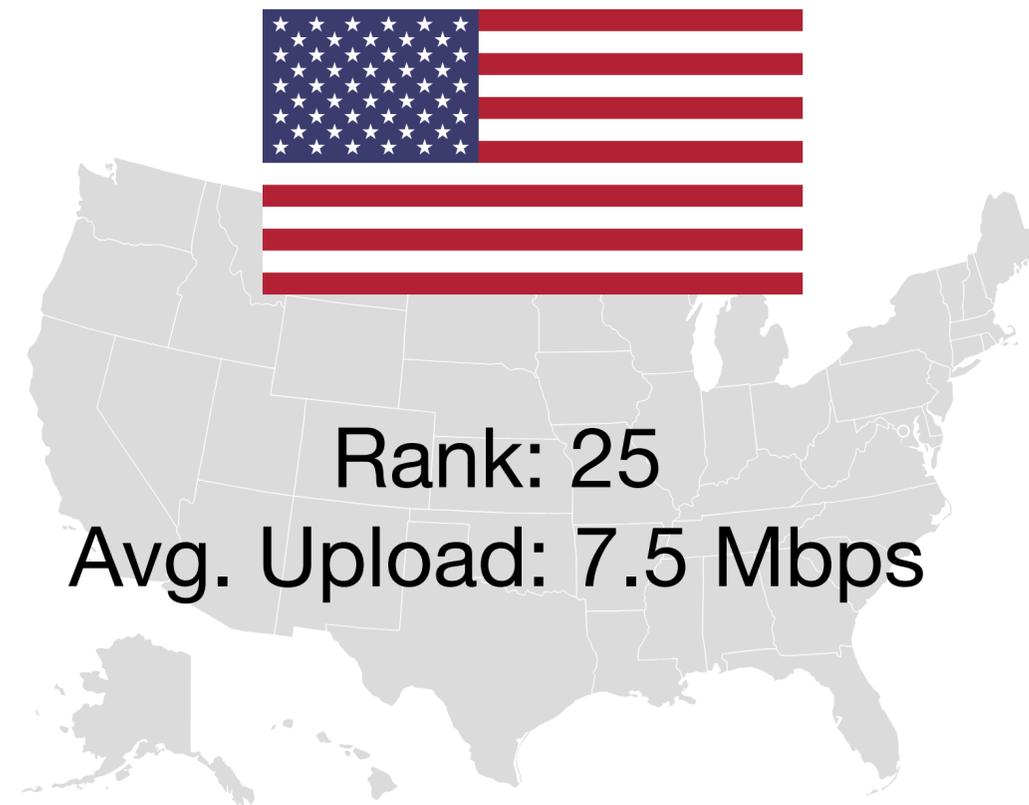
**Multiplier: OT-based**

**Parties: 4**

**Curve: 256-bit**

**2 Mbits**

**sent per party**



source: opensignal

# Example 1: Mobile Wallet

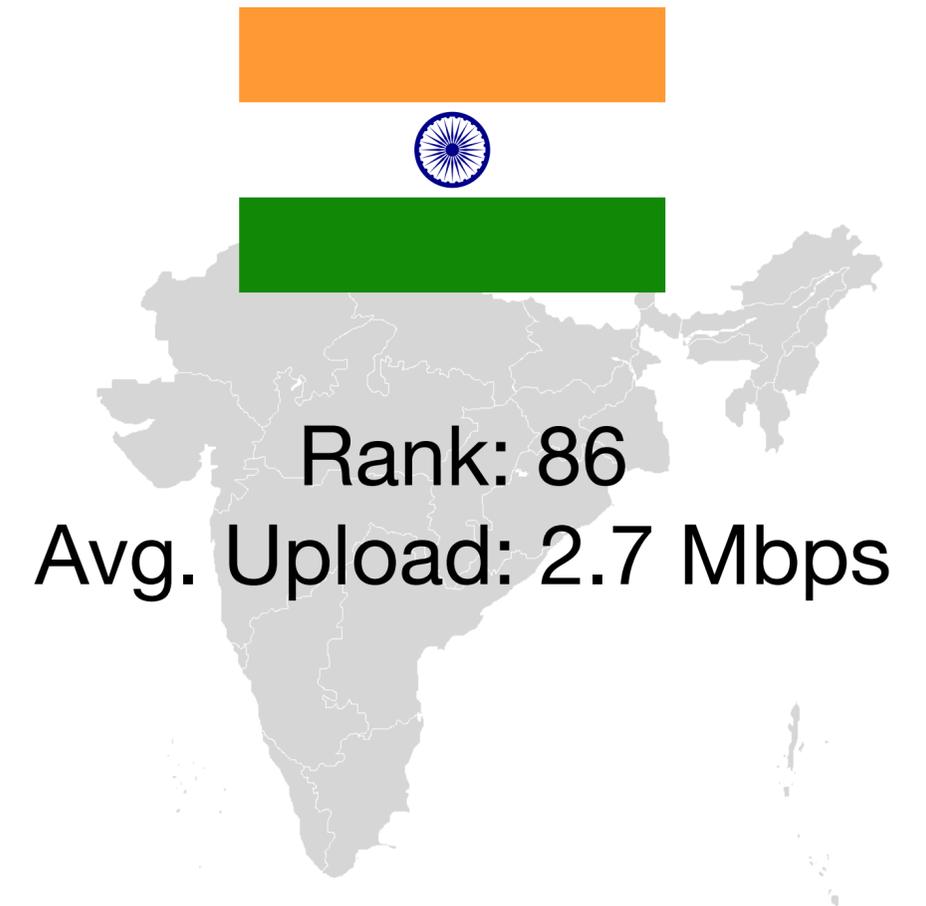
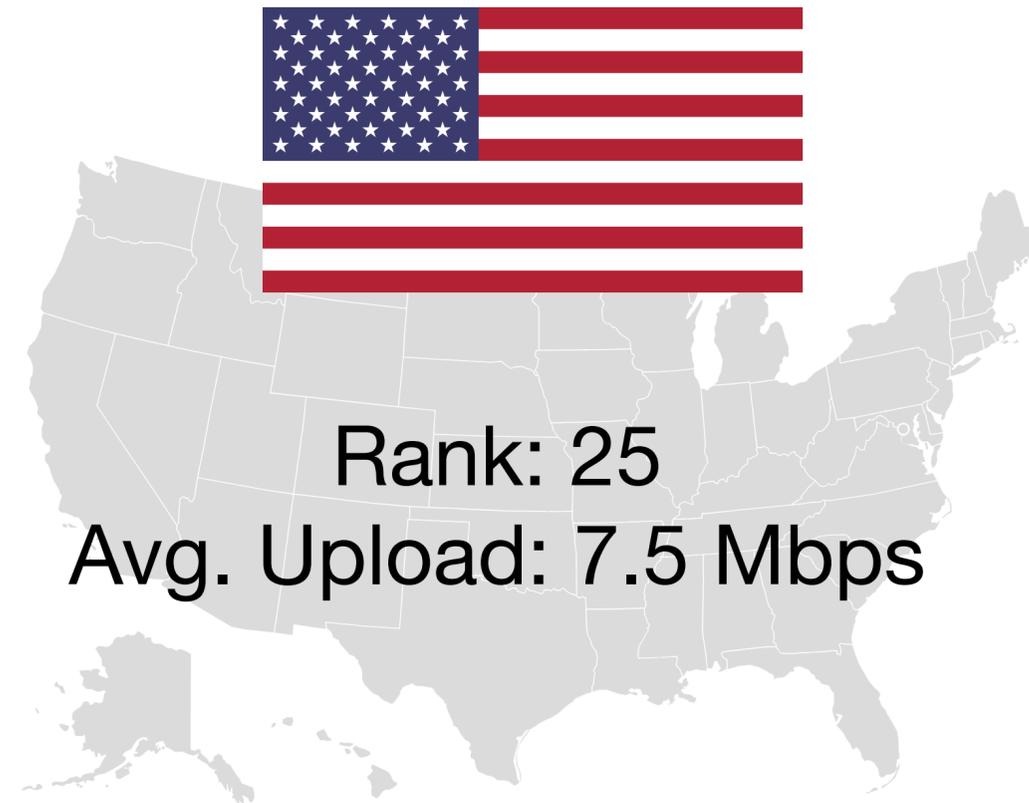
**Multiplier: OT-based**

**Parties: 4**

**Curve: 256-bit**

**2 Mbits**

**sent per party**



source: opensignal

# Example 1: Mobile Wallet

**Multiplier: OT-based**

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source: opensignal

# Example 1: Mobile Wallet

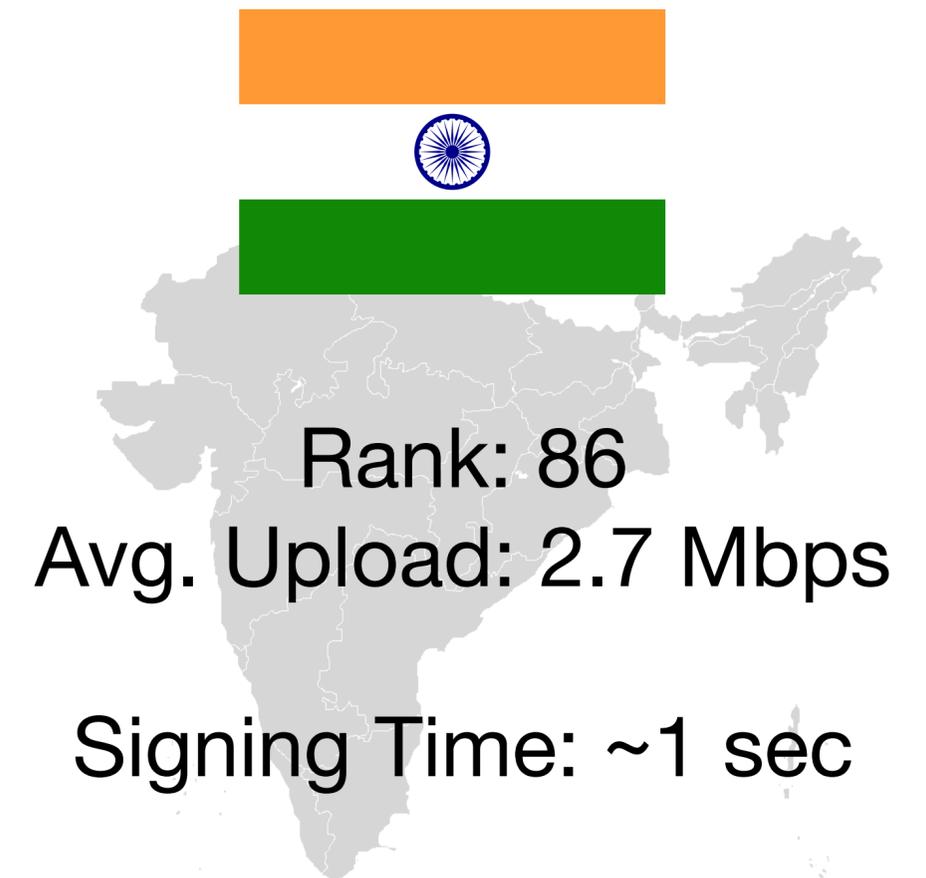
Multiplier: OT-based

Parties: 4

Curve: 256-bit

**2 Mbits**

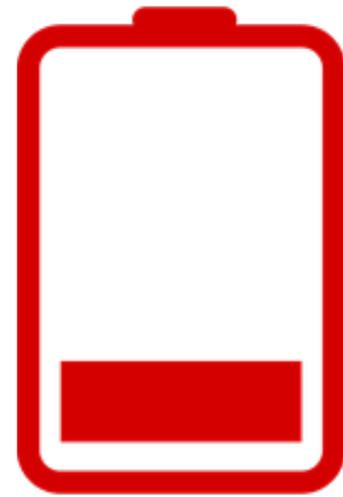
sent per party



Similar to computation time for Paillier  
on powerful hardware!

source: opensignal

# On the Other Hand



Paillier + ZK



OT

# Example 2: Datacenter Signing

How much bandwidth to be CPU bound?  
(including preprocessing)

2 Parties  
~250 sigs/second

256 Parties  
~3 sigs/second

using GCP n1-highcpu nodes

# Example 2: Datacenter Signing

How much bandwidth to be CPU bound?  
(including preprocessing)

2 Parties  
~250 sigs/second

Each party sends:  
~700 Kbits per sig

256 Parties  
~3 sigs/second

Each party sends:  
~185 Mbits per sig

using GCP n1-highcpu nodes

# Example 2: Datacenter Signing

How much bandwidth to be CPU bound?  
(including preprocessing)

2 Parties

~250 sigs/second

Each party sends:  
~700 Kbits per sig

Bandwidth required:  
~180 Mbps symmetric

256 Parties

~3 sigs/second

Each party sends:  
~185 Mbits per sig

Bandwidth required:  
~555 Mbps symmetric

using GCP n1-highcpu nodes

# Summary

Bandwidth isn't always the bottleneck  
or the most important cost factor

Guide concrete optimization by  
studying real use-cases

We ❤️ OT

# Our Protocols

UC Sec From CDH  
in the ROM

OT-Based

No ZK in Signing

One “Online” Msg

Const or Log Round  
Preprocessing

2 Msgs for 2 Parties

Secure Two-Party Threshold ECDSA  
from ECDSA Assumptions

<http://ia.cr/2018/499>

Threshold ECDSA from ECDSA  
Assumptions: the Multiparty Case

<http://ia.cr/2019/523>